



The 20th Annual MARC Conference
Machine Learning, Natural Language Processing, and Psychometrics

Leveraging Process Data in Large-Scale Educational Assessments with Sequence Mining

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Psychometric and Data Science Modeling
Educational Testing Service

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Interactive Items and Process
Data in Large-Scale Assessments



Sequence-Based Methods in
Process Data Analysis



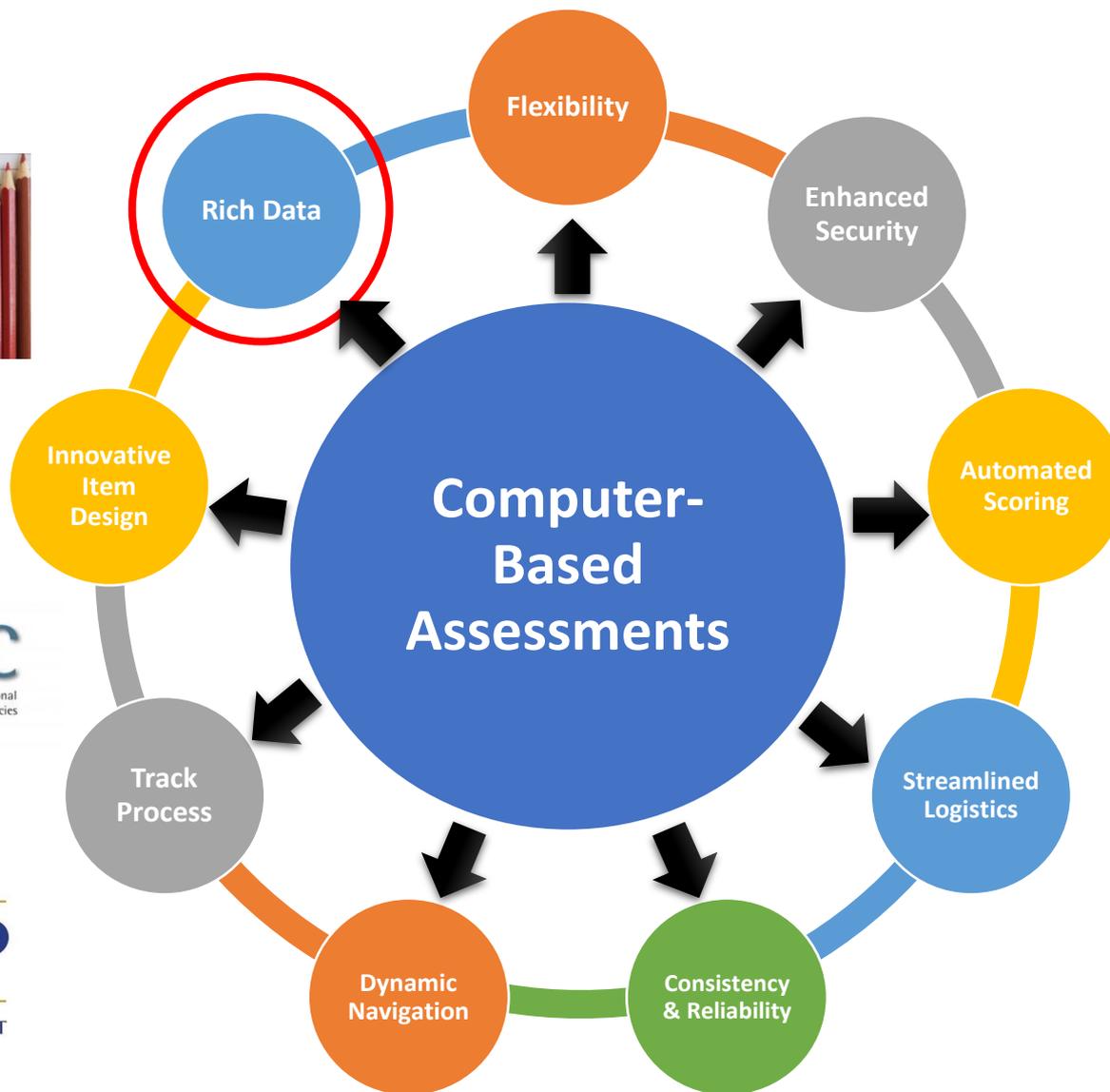
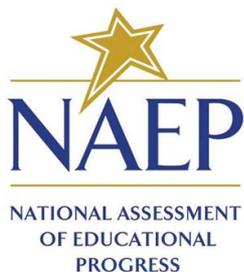
Case Studies: Using Sequence
Mining Techniques in LSA



Discussions and Outlook

Interactive Items and Process Data in Large- Scale Assessments





Mirroring Real-Life Behavior with Interactive Items

- Interactive items are becoming more widely used than in large-scale assessments.
- Recorded time-stamped action sequences contain information on type and order of performed actions as well as the time required on each action.

PISA 2015

Adjustable Glasses

Question 3 / 5

▶ How to Run the Simulation

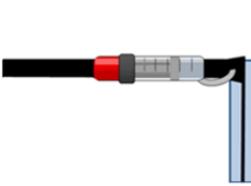
Run the simulation to collect data based on the information below. Select from the drop-down menu to answer the question.

Anna sees both near and distant objects in focus.

How do adjustments to the glasses affect Anna's vision?

Adding fluid to the lens makes objects appear out of focus.

Removing fluid from the lens makes objects appear out of focus.



Anna's View



Amount of Fluid in Lens

Distance from Tree

near midway distant

Run

		Amount of Fluid in Lens				
		-2	-1	0	+1	+2
Distance from Tree	Near					
	Midway					
	Distant					

PISA 2015 Science Inquiry Interactive Item (field trial example item)

A game board is shown.

Some of the squares on the board are labeled.

Drag letters into the rest of the squares so that

- $\frac{1}{3}$ of all the squares on the board are labeled Y.
- $\frac{1}{3}$ of all the squares on the board are labeled B, and
- $\frac{1}{3}$ of all the squares on the board are labeled G.

Y Y B G

Y B G

Clear Answer

*NAEP 2017 Grade 4 Interactive
Math Example Item*

Work Space:10

Time Remaining: 00 mins

Code Blocks

The code blocks in the work space cannot be changed.
Any drone placed on the farm is controlled by the code blocks.
You can click on a drone to change the direction it faces.
Drag and drop the drones so that water is dropped on all of the crop files.

Click [] to see how the drone on the farm drops water on the crop files.
Click [] when you are ready to continue.

*ICILS2018 Computational
Thinking Interactive Program
Coding Example Item*

PISA 2015

Xandar - Introduction

Part 3 - Directions

Who's in the Chat

YOU Alice Zach

Alice: We got one - let's keep going!

Whoever answered a Geography question, nice work!

Since somebody answered a Geography question, I'm going to switch subjects!

I should answer the Geography questions. Let's work on the subjects we chose.

Send

Scorecard

Geography	People	Economy
<input checked="" type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>
<input type="checkbox"/>	<input type="checkbox"/>	<input type="checkbox"/>

Geography People Economy

What is Xandar's longest river? Kurlu River

What is Xandar's tallest mountain?

What is Xandar's rainy season?

What proportion of Xandar is desert?

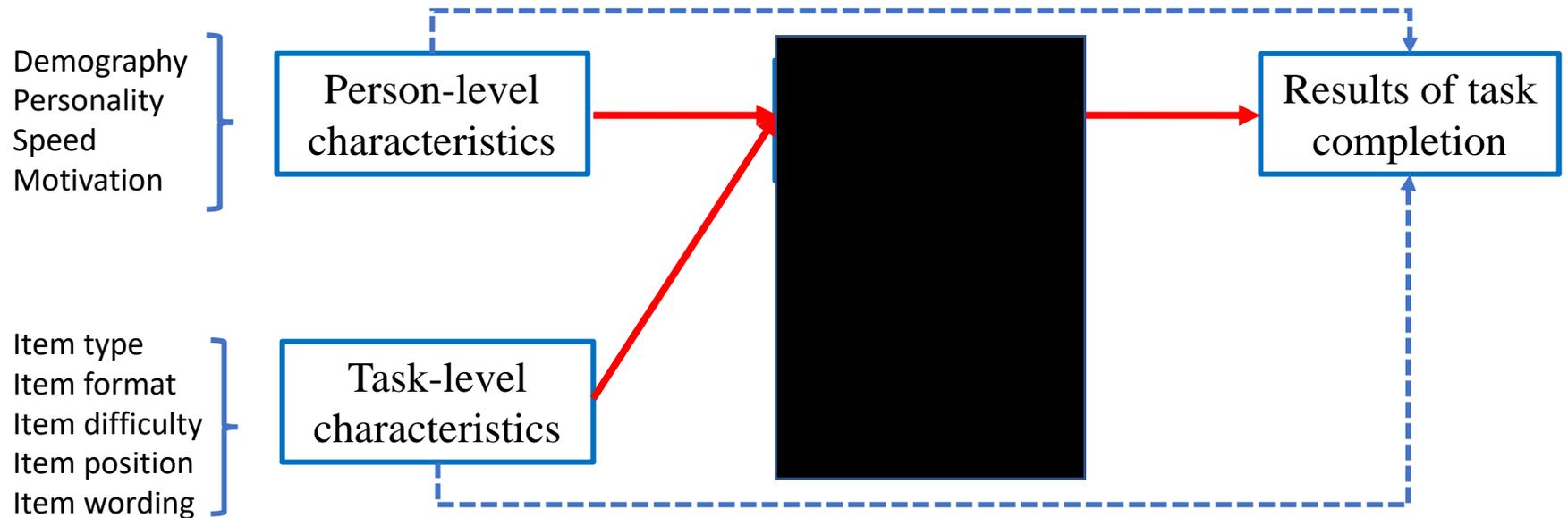
*PISA 2015 Collaborative
Problem-Solving Example Item*

Examples from Different Subjects

Why Does Response Process Matter?

- Response process brings additional information and be helpful for aspects below:
 - **Task construction**
 - Investigating whether examinees interact with interactive tasks as intended
 - **Invariance explorations**
 - Defining invariance between group not only in terms of item difficulty but also in terms of the processes applied for solving a given task
 - **Richer description of performance**
 - Investigating not only whether examinees could solve a given task but also whether they did so efficiently and systematically
 - **Refining theories on response processes to interactive tasks**
 - **Designing tailored interventions**
 - Identifying subskills or meta competencies that examinees are lacking

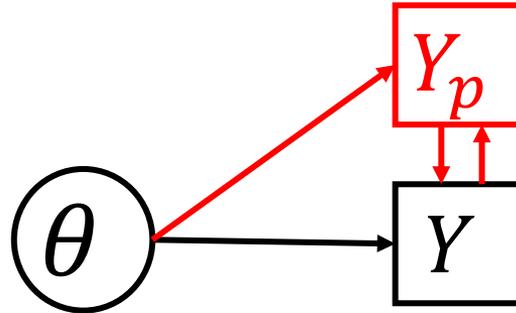
A Typical Assessing Process



Heldt et al. (2020)

What is in the Black Box?

Process data



- An enormous amount of unstructured data is collected (even worse considering both performed actions and the associated time stamps).
- Potentially rich source of information on examinee behavior, leveraging its potential by meaningful aggregation is not trivial
- Calls for new methods with incorporation of data science and analytics techniques, to re-shape the future of measurement.

Sequence-Based Methods in Process Data Analysis



Sequence Mining

- Sequential pattern mining is a topic of data mining concerned with finding statistically relevant patterns between data examples where the values are delivered in a sequence.
- Sequence mining techniques include building efficient databases and indexes for sequence information, extracting the frequently occurring patterns, comparing sequences for similarity, and recovering missing sequence members.

Dong & Pei, 2007

Sequence-Based Methods in Process Data Analysis

Text and “real” clickstreams as commonly encountered types of unstructured sequence data. Borrow from sequence mining, natural language processing (NLP), and machine learning

Mini-Sequences (n-grams)

- Disassemble long sequence into manageable short pieces extracted as features in prediction and clustering

Pairwise Sequence Similarity Measures

- Take the sequence as a whole and compute the distance between each pair to create new variables for prediction and clustering

Latent Sequence Modeling

- From observed sequences to derive the latent sequence transition stage and probability

Mini Sequences (n-grams)

I am happy to give a talk today.

unigrams

bigrams

trigrams

Action sequence: STRT, SS, SS_Type_FN, E, E_S, Next, Next_OK, END

Unigrams (8) "START", "SS", "SS_Type_FN", "E", "E_S", "Next", "Next_OK", "END"

Bigrams (7) "START, SS", "SS, SS_Type_FN", "SS_Type_FN, E", "E, E_S", "E_S, Next",
"Next, Next_OK", "Next_OK, END"

Trigram (6) "START, SS, SS_Type_FN", "SS, SS_Type_FN, E", "SS_Type_FN, E, E_S",
"E, E_S, Next", "E_S, Next, Next_OK", "Next, Next_OK, END"

Mini Sequences (n-grams)

- Using n-grams and robust feature selection method (e.g., χ^2 selection) to identify behavioral patterns that distinguish between groups (He & von Davier, 2015, 2016)
- Using machine learning techniques for selecting key action features for predicting group membership (e.g., correctness group) (Han et al., 2019; Salles et al., 2020; Stadler et al., 2019; Ulitzsch et al., 2022)
- Using event history models for identifying key features for predicting the timing and correctness of task completion (e.g., Chen et al., 2019; Han et al., 2019)
- Using dynamic action sequence to predict whether the problem-solving process is on track (Ulitzsch et al., 2022)

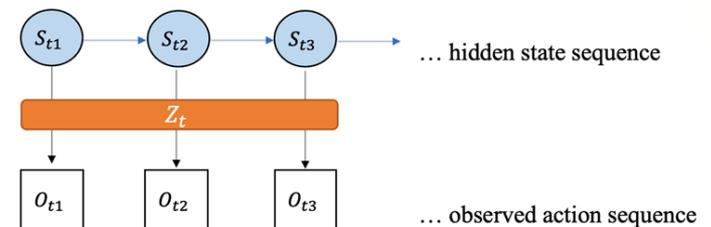
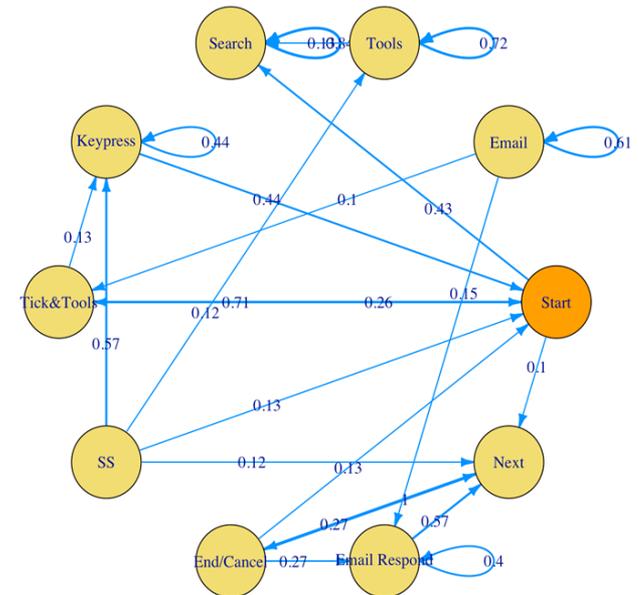
Cons: Breaking up action sequences into short n-gram sequences could exploit meaningful information such as dependencies between actions

Pairwise Sequence Similarity

- **Sequence similarity to be compared with pre-defined sequences or compute pairwise distance matrix**
 - Generating efficiency and similarity indicators with longest common subsequence (LCS) (He et al., 2019, 2021)
 - Determining the similarity between students' strategies with correct ones with edit distance (Hao et al., 2015)
- **Sequence similarity with incorporation of timing information**
 - Determining common behavioral patterns in terms of the performed actions and the time elapsed in between with LCS (Ulitzsch et al, 2021; Ulitzsch, He & Pohl, 2022)
 - Clustering navigation patterns with dynamic time warping method (He et al., 2022)
- **Dimensionality reduction and latent feature extraction**
 - Using distance measures and multidimensional scaling for parsimonious descriptions of behavioral patterns (Tang et al., 2019)
 - Deep learning from observed sequence to latent sequence features (Tang et al., 2020)

Latent Sequence Modeling

- The hidden Markov model (HMM) that has been widely used in NLP and speech recognition are also applicable in process data to extract latent states of the problem-solving process and investigate how these latent states are transitioned (Xiao et al., 2021; He et al., in preparation)
- Multigroup HMM provides the possibility to compare the transition probability between groups under the common latent sequence model (He et al., in preparation)
- Supports parsimonious modeling and description of behavioral pathways



(He, Bei, & Jiang, in preparation)

Case studies: Using Sequence Mining Techniques in Large- Scale Assessments





Clustering Reading Navigation Sequences with Dynamic Time Warping Method

In collaboration with

Dr. Francesca Borgonovi, OECD, University College London

Dr. Javier Suarez-Alvarez, University of Massachusetts

He, Q., Borgonovi, F., Suárez-Álvarez, J. (2022). Clustering Sequential Navigation Patterns in Multiple-Source Reading Tasks with Dynamic Time Warping Method. Journal of Computer-Assisted Learning. DOI: [10.1111/jcal.12748](https://doi.org/10.1111/jcal.12748)



Navigation is recognized as a key component of reading in the digital environment as readers “construct” their text through navigation and spend time retrieving information from eventually targeted texts.

Good readers tend to

- minimize their visits to irrelevant pages;
- locate necessary pages efficiently;
- choose strategies that are suited to the demands of individual tasks.

Dynamic Navigation

- The description of readers' navigation process demands tremendous support from log files.
- Data-driven investigations of how students transit pages in digital reading tasks and how much time they spend on each transition allow mapping sequences of navigation behaviors into students' navigation reading strategies.



Multiple Source and Dynamic Texts in PISA Reading

- Searching across multiple documents
- Integrating across texts for inferences
- Assessing the credibility of sources
- Handling conflicting information



Blog Book Review Science News
www.theprofessorblog.com/fieldwork/RapaNui

The Professor's Blog

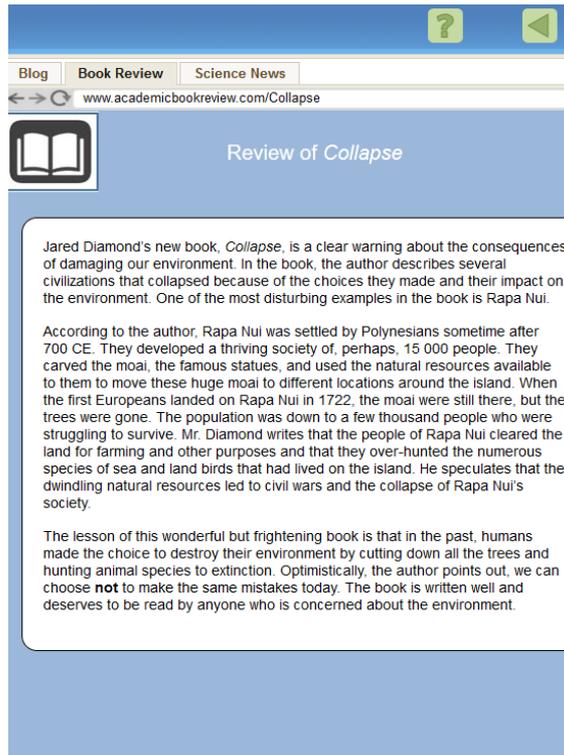
Posted May 23, 11:22 a.m.

As I look out of my window this morning, I see the landscape I have learned to love here on Rapa Nui, which is known in some places by the name Easter Island. The grasses and shrubs are green, the sky is blue, and the old, now extinct volcanoes rise up in the background.

I am a bit sad knowing that this is my last week on the island. I have finished my field work and will be returning home. Later today, I will take a walk through the hills and say good-bye to the moai that I have been studying for the past few months. Here is a picture of some of these massive statues.



If you have been following my blog this year, then you know that the people of Rapa Nui carved these moai hundreds of years ago. These impressive statues have been carved in a single quarry on the eastern part of the island. Some of the statues are made of basalt, and the people of Rapa Nui were able to move



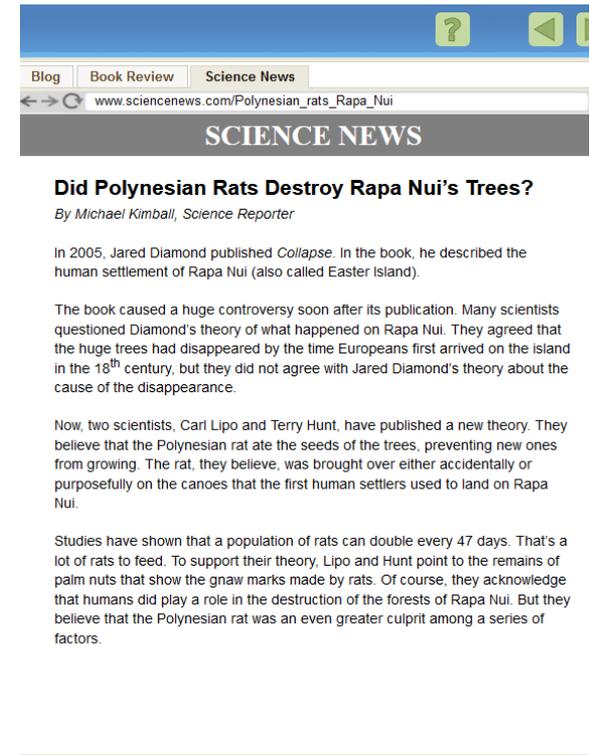
Blog Book Review Science News
www.academicbookreview.com/Collapse

Review of Collapse

Jared Diamond's new book, *Collapse*, is a clear warning about the consequences of damaging our environment. In the book, the author describes several civilizations that collapsed because of the choices they made and their impact on the environment. One of the most disturbing examples in the book is Rapa Nui.

According to the author, Rapa Nui was settled by Polynesians sometime after 700 CE. They developed a thriving society of, perhaps, 15 000 people. They carved the moai, the famous statues, and used the natural resources available to them to move these huge moai to different locations around the island. When the first Europeans landed on Rapa Nui in 1722, the moai were still there, but the trees were gone. The population was down to a few thousand people who were struggling to survive. Mr. Diamond writes that the people of Rapa Nui cleared the land for farming and other purposes and that they over-hunted the numerous species of sea and land birds that had lived on the island. He speculates that the dwindling natural resources led to civil wars and the collapse of Rapa Nui's society.

The lesson of this wonderful but frightening book is that in the past, humans made the choice to destroy their environment by cutting down all the trees and hunting animal species to extinction. Optimistically, the author points out, we can choose **not** to make the same mistakes today. The book is written well and deserves to be read by anyone who is concerned about the environment.



Blog Book Review Science News
www.sciencenews.com/Polynesian_rats_Rapa_Nui

SCIENCE NEWS

Did Polynesian Rats Destroy Rapa Nui's Trees?

By Michael Kimball, Science Reporter

In 2005, Jared Diamond published *Collapse*. In the book, he described the human settlement of Rapa Nui (also called Easter Island).

The book caused a huge controversy soon after its publication. Many scientists questioned Diamond's theory of what happened on Rapa Nui. They agreed that the huge trees had disappeared by the time Europeans first arrived on the island in the 18th century, but they did not agree with Jared Diamond's theory about the cause of the disappearance.

Now, two scientists, Carl Lipo and Terry Hunt, have published a new theory. They believe that the Polynesian rat ate the seeds of the trees, preventing new ones from growing. The rat, they believe, was brought over either accidentally or purposefully on the canoes that the first human settlers used to land on Rapa Nui.

Studies have shown that a population of rats can double every 47 days. That's a lot of rats to feed. To support their theory, Lipo and Hunt point to the remains of palm nuts that show the gnaw marks made by rats. Of course, they acknowledge that humans did play a role in the destruction of the forests of Rapa Nui. But they believe that the Polynesian rat was an even greater culprit among a series of factors.

Aims

- To identify students' navigation patterns in multiple-source reading tasks using a sequence clustering approach
- To examine how students' navigation patterns are associated with their reading performance and socio-demographic characteristics
- To showcase how the navigation sequences could be clustered on the similarity measure by dynamic time warping (DTW) methods

Dataset

- A sample of 16,957 students from 69 countries participating in the PISA 2018
- Executed **at least one navigation activity** (i.e., visited at least one page beyond the default homepage) in one example task (CR551Q11) in the reading Rapa Nui unit
- Demographics:
 - 56.1% of the students were girls, which was a bit higher than the 52% of girls in the full sample in this reading unit.
 - The index of economic, social, and cultural status (ESCS) was 0.245 in this subsample, which was also marginally higher than that of the full sample (-0.05) in this reading unit.

Instrument

PISA 2018

Rapa Nui
Question 7 / 7

Refer to all three sources on the right by clicking on each of the tabs. Type your answer to the question.

After reading the three sources, what do you think caused the disappearance of the large trees on Rapa Nui? Provide specific information from the sources to support your answer.

Blog Book Review Science News
www.theprofessorblog.com/fieldwork/RapaNui

The Professor's Blog

Posted May 23, 11:22 a.m.

As I look out of my window this morning, I see the landscape I have learned to love here on Rapa Nui, which is known in some places by the name Easter Island. The grasses and shrubs are green, the sky is blue, and the old, now extinct volcanoes rise up in the background.

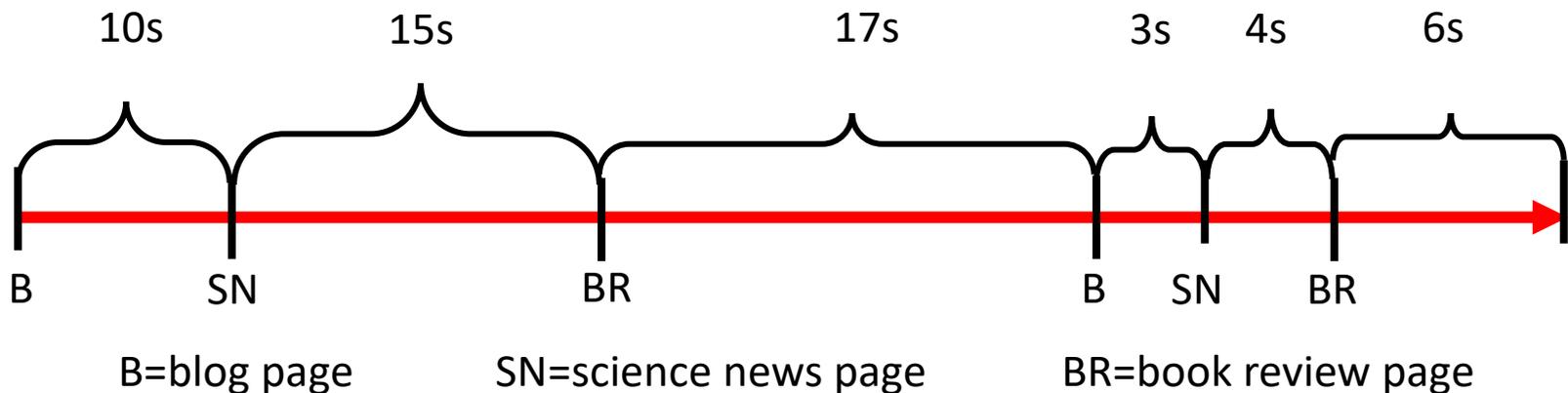
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If you have been following my blog this year, then you know that the people of Rapa Nui carved these moai hundreds of years ago. These impressive moai had been carved in a single quarry on the eastern part of the island. Some of them weighed thousands of kil...

Clickstream Data

- Students' navigation sequences were characterized by two indicators:
 - Page sequence that tracks the page transition path
 - Time sequence that records the time duration on each visited page.



Page sequence: {B, SN, BR, B, SN, BR, END}

Time sequence: {10, 15, 17, 3, 4, 6}

Research Design

- **Step 1: Similarity measure**

- Pairwise sequence distance computation with dynamic time warping (DTW) method
- Execute by page sequence and time sequence respectively

- **Step 2: Sequence clustering (unsupervised machine learning)**

- K-medoid partitioning clustering analyses on sequence distance matrix

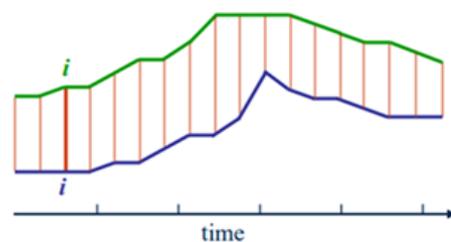
Step 1: Similarity Measure by DTW

- Dynamic time warping (Sakoe & Chiba, 1978) is a distance measure that searches the optimal warping path between two series.

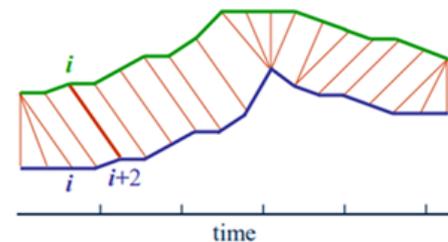
- Given sequences

$X = \{x_1, x_2, \dots, x_n\}$ and

$Y = \{y_1, y_2, \dots, y_m\}$ with the same or different lengths, a warping path W is an alignment between X and Y , involving one-to-many mappings for each pair of elements.

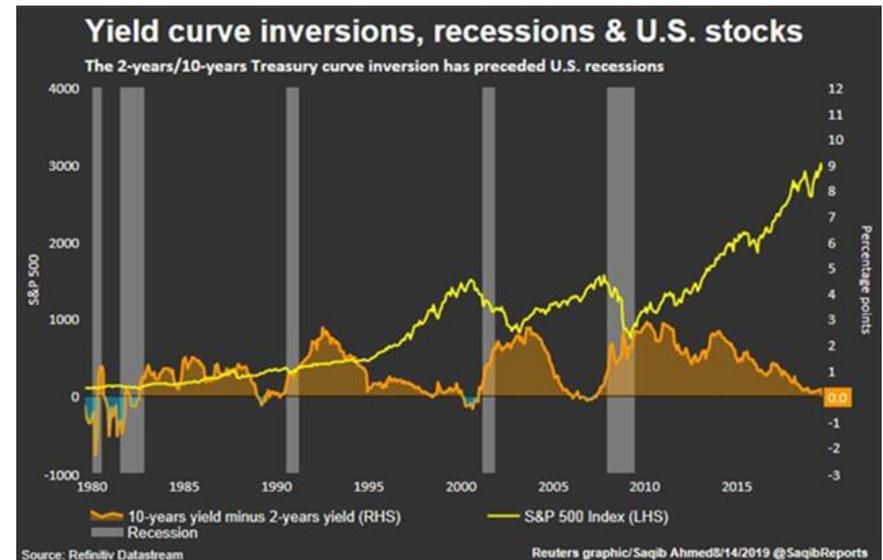
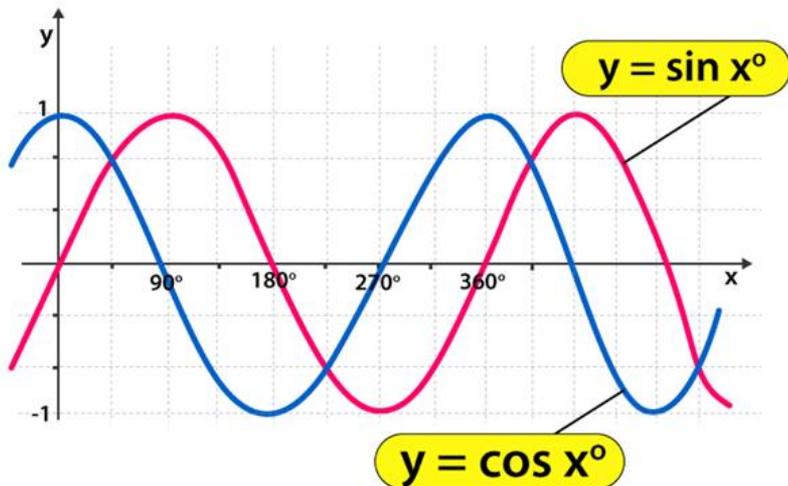


Any distance (Euclidean, Manhattan, ...) which aligns the i -th point on one time series with the i -th point on the other will produce a **poor similarity score**.



A non-linear (elastic) alignment produces a **more intuitive similarity measure**, allowing similar shapes to match even if they are out of phase in the time axis.

Reasons to Use DTW



Dynamic Time Warping Algorithm

- The initial step of DTW algorithm is defined as:

$$DTW(i, j) = \begin{cases} \infty & \text{if } (i = 0 \text{ or } j = 0) \text{ and } i \neq j \\ 0 & \text{if } i = j = 0 \end{cases}$$

- The recursive function of DTW is defined as

$$DTW(i, j) = \min \begin{cases} DTW(i - 1, j) + w_h C(i, j) \\ DTW(i, j - 1) + w_v C(i, j) \\ DTW(i - 1, j - 1) + w_d C(i, j) \end{cases}$$

where (w_h, w_v, w_d) are weights for the horizontal, vertical and diagonal directions, respectively. $DTW(i, j)$ denotes the distance or cost between two sub-sequences $\{x_1, x_2, \dots, x_i\}$ and $\{y_1, y_2, \dots, y_j\}$, and $DTW(N, M)$ indicates the total cost of the optimal warping path.

	5	10	6	3	1	2	4	3
	4	6	3	1	0	1	3	3
A	3	3	1	0	1	1	2	4
	2	1	0	1	3	4	4	7
	1	0	1	3	6	8	9	13
		1	2	3	4	3	2	5
		B						

$A_i = \{1, 2, 3, 4, 5\}$

$B_j = \{1, 2, 3, 4, 3, 2, 5\}$

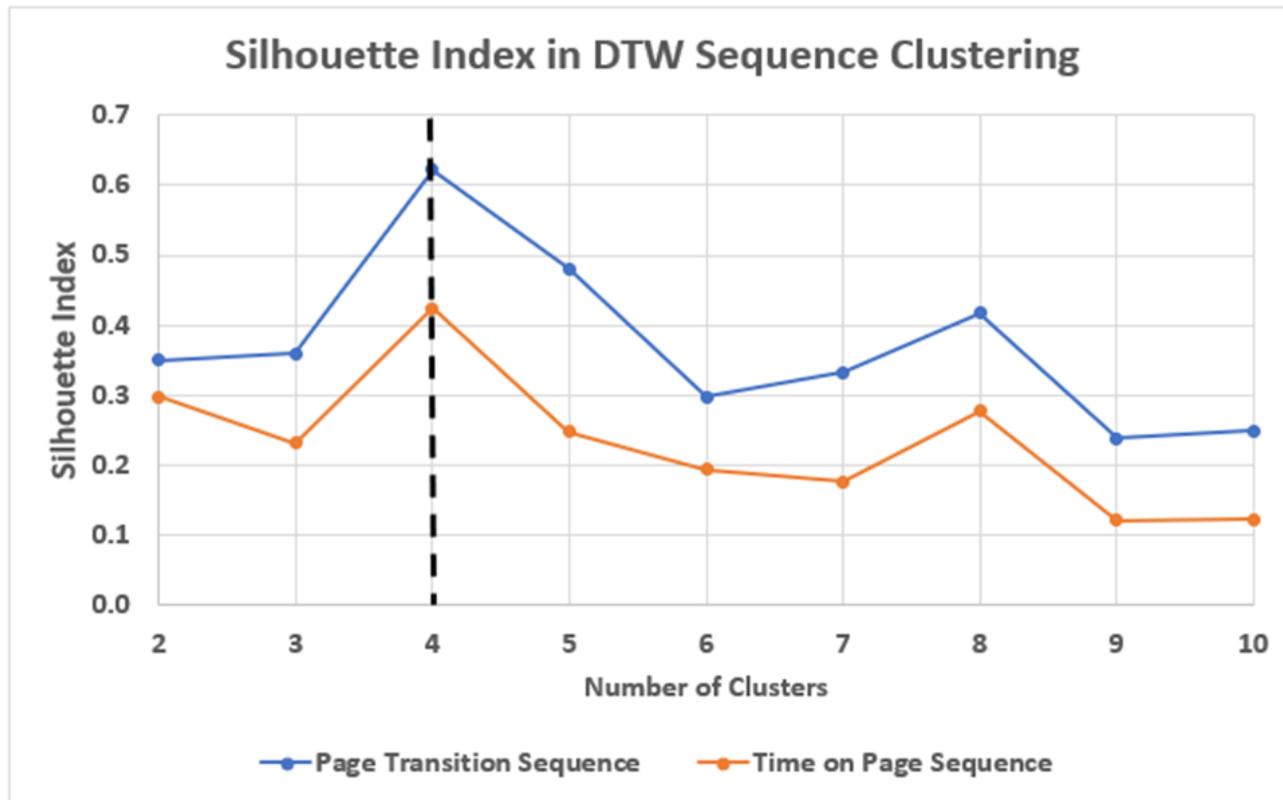
$dtw(i, j) = |A_i - B_j| + \min(D[i - 1, j - 1], D[i - 1, j], D[i, j - 1])$

Recode categorical variables to numeric variables (define B=1, BR=2, SN=3)

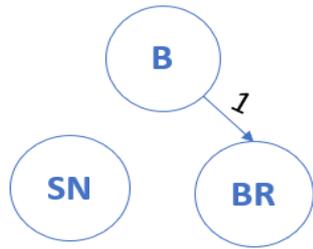
Step 2: Sequence Clustering

- K-medoids is a classical partitioning technique of clustering that splits the data set of n objects into k clusters, where the number k of clusters assumed known a priori.
- In this study, we set k as 2 to 10 to as a priori and set the optimal number of clusters k with the silhouette index (Rousseeuw, 1987).
- The silhouette index ranges from -1 to $+1$, where a high value indicates that the object is well matched to its own cluster and poorly matched to neighboring clusters.

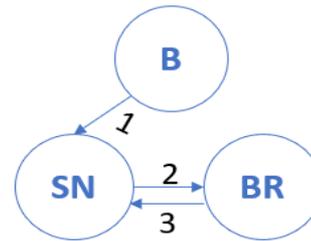
Silhouette Index for Optimal Number of Clusters



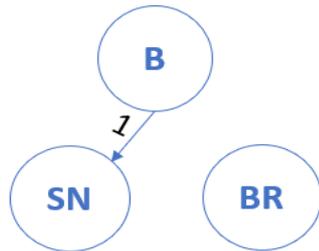
Result 1: Page Sequence Clustering



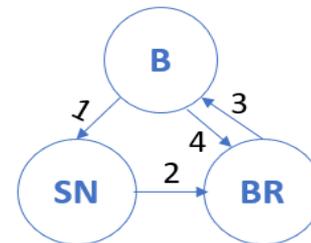
P1



P2



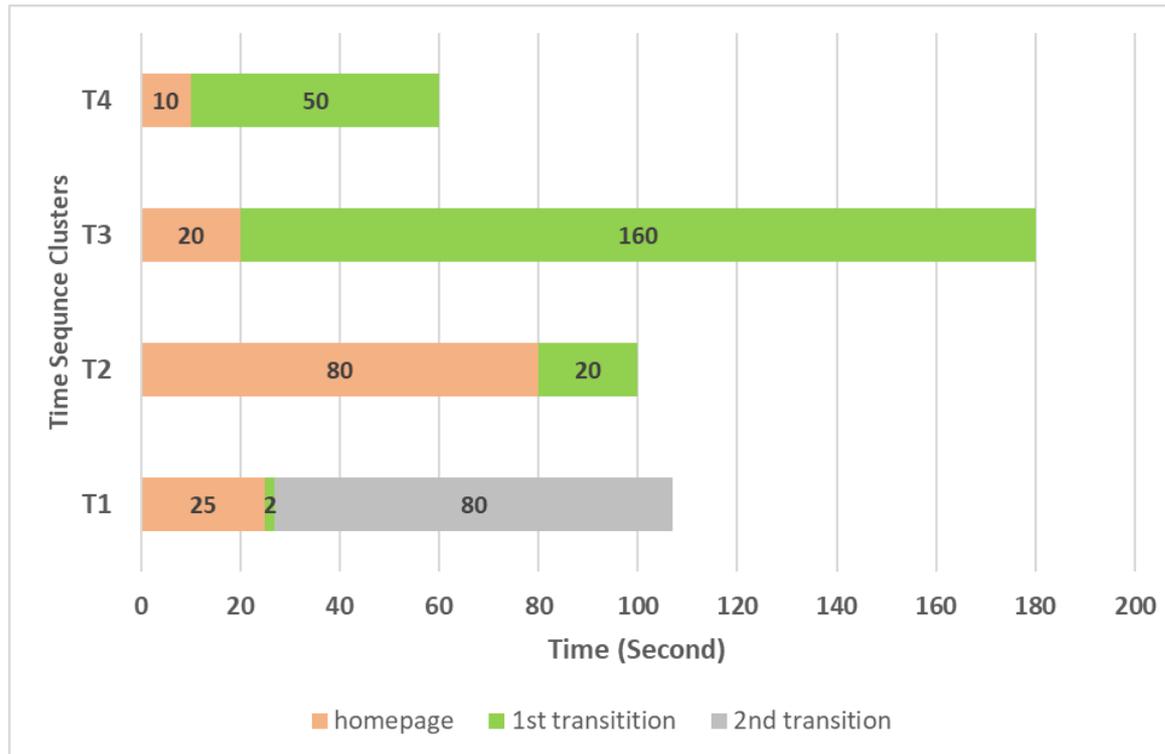
P3



P4

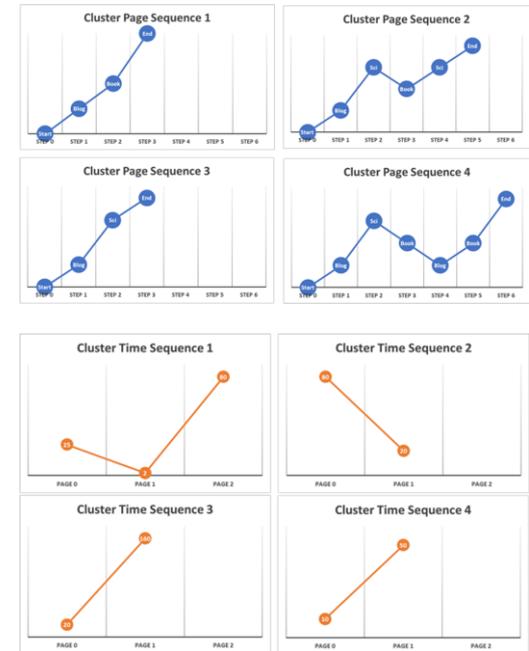
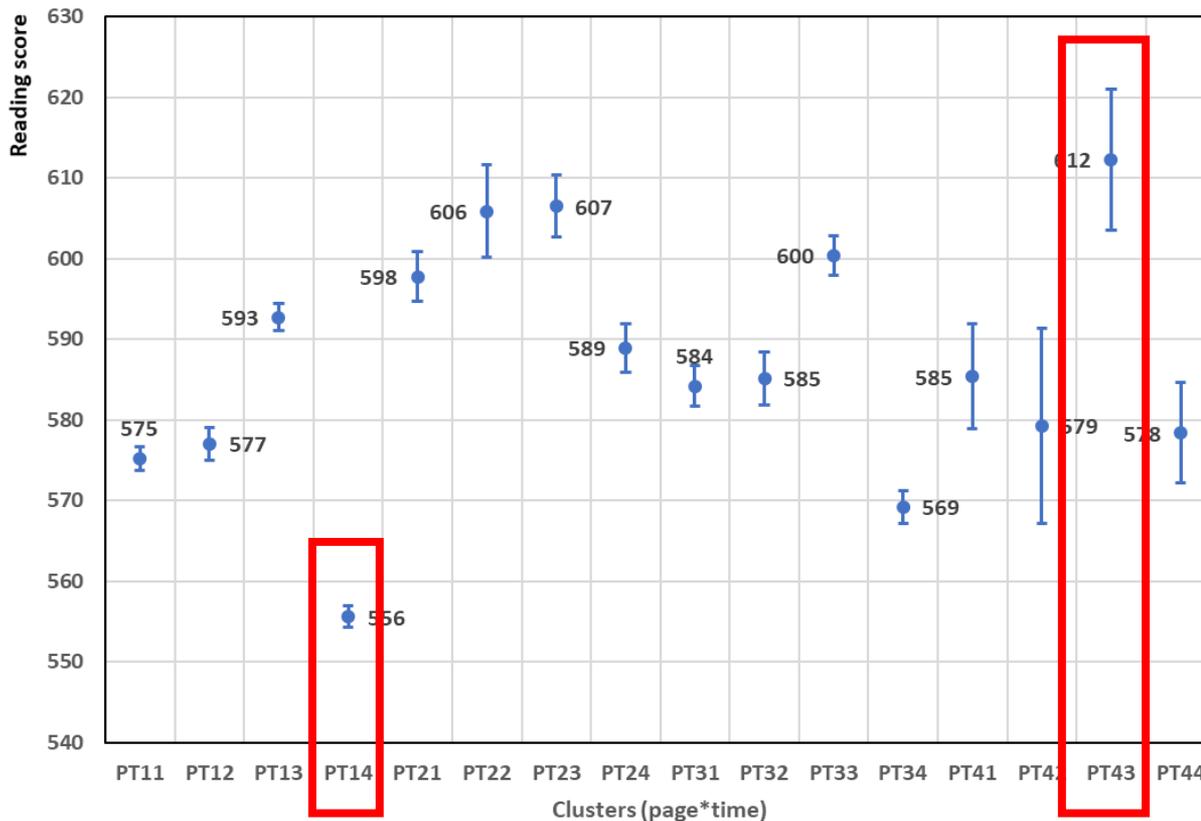
Clusters	Sample Size	Percentage	Reading Proficiency Score			Gender		Socio-Economic Index		
			Mean	S.D.	S.E.	Girl (%)	Boy (%)	Mean	S.D.	S.E.
P1	11091	65.4%	574.13	82.05	0.78	65.2%	66%	0.22	0.94	0.01
P2	1952	11.5%	599.06	76.97	1.74	11.4%	12%	0.29	0.90	0.02
P3	3438	20.8%	585.07	72.38	1.23	20.8%	20%	0.28	0.92	0.02
P4	476	2.6%	587.75	85.03	3.90	2.6%	3%	0.28	0.92	0.04

Result 2: Time Sequence Clustering



Clusters	Sample Size	Percentage	Reading Proficiency Score			Gender		Socio-Economic Index		
			Mean	S.D.	S.E.	Girl (%)	Boy (%)	Mean	S.D.	S.E.
T1	4651	27.4%	582.72	78.12	1.15	28.1%	27%	0.27	0.93	0.01
T2	2385	13.6%	583.75	79.43	1.63	13.6%	15%	0.33	0.92	0.02
T3	3675	23.5%	598.36	77.17	1.27	23.5%	19%	0.31	0.91	0.02
T4	6246	34.8%	564.66	80.83	1.02	34.8%	39%	0.16	0.94	0.01

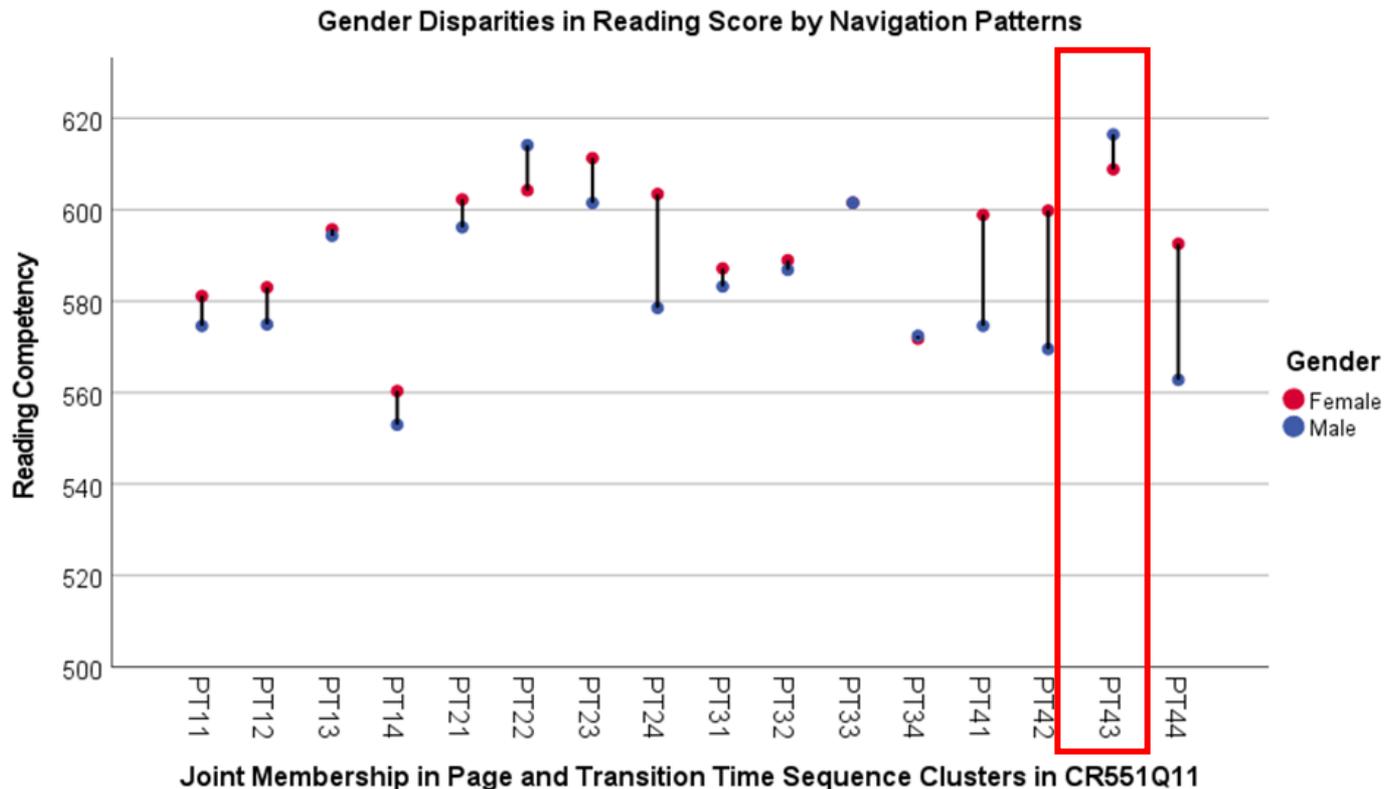
Result 3: Association Between Navigation Patterns and Reading Skills



Result 4: Gender Disparities

Girls were more likely to achieve higher scores than boys when longer navigation sequences were used with shorter reading time on transited pages.

However, boys were more likely to achieve higher scores than girls when they spent longer time reading either homepage or transited page along with comprehensive navigation paths through the multiple pages.



Summary

- This study draws on sequential process data from a multiple-source reading task to showcase how students' navigation strategies could be identified via sequence clustering on the DTW similarity measure.
- The DTW method features in identifying the optimal warping path between the two sequences, which cares more about the sequence shapes across time windows.
- The navigation sequence patterns were moderately associated with students' reading proficiency levels.
- Students who visited all the pages and spent more time reading without rush transitions scored higher in reading than those students with less focused navigation.



Evaluating Consistency of Behavioral Patterns Across Multiple Tasks Using Process Data

An Empirical Study in PIAAC

In collaboration with
Dr. Dandan Liao, Cambium Assessment
Dr. Hok Kan Ling, Queen's University
Dr. Hong Jiao, University of Maryland

He, Q., Liao, D., Ling, H. K., & Jiao, H. (accepted). Evaluating Consistency of Behavioral Patterns across Multiple Tasks Using Process Data: A case study in PIAAC. Invited book chapter in forthcoming book L. Khorramdel, M. von Davier, K. Yamamoto. (Eds.) *Innovative Computer-based International Large-Scale Assessments – Foundations, Methodologies and Quality Assurance Procedures*. Springer.

PIAAC

- The Programme for the International Assessment of Adult Competencies (PIAAC) is the first International study with a focus on assessing adults' skills carried out by OECD.
- Assess the cognitive and workplace skills of working-age (16 – 65 years) individuals worldwide.
- Problem Solving in Technology-Rich Environments (PSTRE)



Introduction

- Because of the complexity and high dimensional structure of process data, most studies focus on analyzing **one single** item. (e.g., He & von Davier, 2016; Han et al., 2019; Ulitzsch et al., 2021)
- Evaluating the behavioral consistency across items renders possible capturing and modeling person-related latent characteristics. (e.g., Liao et al., 2019; He et al., 2019, 2021)

Education & Skills Online

Unit 6

You ordered a desk lamp from KE-Lamps.com.

The desk lamp arrived, but it was not the color you ordered.

Using the company's website, arrange to exchange the lamp you received for the one you ordered.

Once you have finished, click Next to go on.

KE-Lamps.com
The best way to light your life

Bedroom Lamps
Desk Lamps
Floor Lamps
Table Lamps
New Arrivals
SALE!

Customer Comments Customer Service Employment Opportunities About Us

OECD PIAAC Section 1

Unit 22

You want to copy some music files to your portable music player.

The music player has room for 20 MB and you want as many files as possible. You want to include only jazz and rock music.

Select the files to include.

Once you have selected the files, click Next to continue.

Title	Size	Time	Artist	Genre
<input type="checkbox"/> A Foreign Affair	14.8 MB	11:40	Don Rader Quartet	Jazz
<input type="checkbox"/> About the Blues	4.3 MB	3:08	Julie London	Blues
<input type="checkbox"/> Another Mind	7.8 MB	8:44	Heleni Lekara	Jazz
<input type="checkbox"/> Blue Trane	10 MB	9:03	John Coltrane	Jazz
<input type="checkbox"/> Don't Give up on Me	3.5 MB	3:45	Solomon Burke	Blues
<input type="checkbox"/> Far Out	5.3 MB	5:25	Antonio Faraó	Jazz
<input type="checkbox"/> Fire and Water	5.3 MB	4:00	Free	Blues
<input type="checkbox"/> If	4.9 MB	5:48	Myriam Aler	Jazz
<input type="checkbox"/> K	2.2 MB	3:04	INXS	Rock
<input type="checkbox"/> Indeed	7.1 MB	5:59	Carol Welsman	Jazz
<input type="checkbox"/> On an Island	16 MB	6:47	David Gilmore	Blues
<input type="checkbox"/> Pass It On	3.1 MB	3:36	Albert Cayo	Jazz
<input type="checkbox"/> Raindrops, Raindrops	5.2 MB	3:46	Karin Krog	Jazz
<input type="checkbox"/> Say You Will	8.8 MB	3:47	Fleetwood Mac	Rock
<input type="checkbox"/> Skin Deep	7.1 MB	4:28	Buddy Guy	Blues
<input type="checkbox"/> Speak No Evil	6.9 MB	5:13	Flora Purim	Jazz
<input type="checkbox"/> The Other Side of Blue	6.5 MB	5:08	Jean Stry & Jobo	Jazz
<input type="checkbox"/> The Rise	7.3 MB	7:28	Julien Lourau	Jazz
<input type="checkbox"/> The Rising	4.5 MB	4:50	Bruce Springsteen	Rock

Total Size Selected (MB) 20

Research Objectives

- To investigate whether the consistent behavioral patterns could be identified by process data features
- To examine the association among the consistency of behavioral patterns with cognitive competency and background variables.



What are the consistent behavioral patterns?



What kind of people are in each behavioral pattern?

Three sub-studies

Study 1:

Using aggregate-level response process variables: number of actions and response time.

Study 2:

Using action sequences with similarity computation.

Study 3:

Mapping the behavioral patterns by problem-solving competency and background variables.

Sample

- A total of 1,340 test takers in the U.S. sample
- Routed to the second module of PSTRE items in PIAAC 2012.
- 629 female test takers (46.9%) and 711 male test takers (53.1%).
- The mean age was 39.2 years (SD = 14.0).
- 680 test takers (50.7%) had an educational level above high school.
- Three cases had technical issues, removed
- 1,337 test takers in the final sample.



Study 1: Using Aggregate Level Variables (number of actions, total response time)



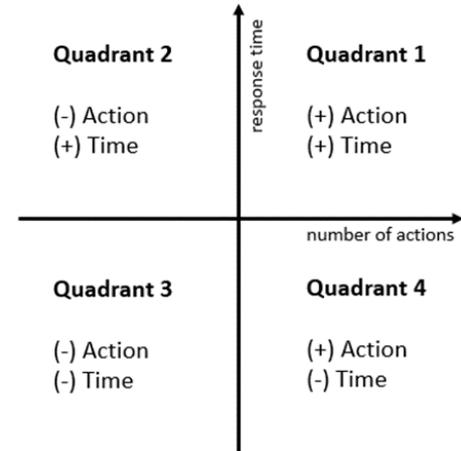
Why These Two Variables?

- The number of actions and response time bear important information on behavioral patterns.
- Evidence has shown that response time is highly correlated with the problem-solving process, skipping behaviors, engagement, and performance (e.g., Ulitzsch et al., 2019; de Boeck & Jeon, 2019; Goldhammer et al., 2014; Liao et al., 2020; Naumann & Goldhammer, 2017; Sahin & Colvin, 2020).
- The variables response time and the number of actions were found as the most informative factors in a previous cluster analysis of respondents' behaviors using the same sample (He, Liao, & Jiao, 2019).

Study 1: Using Aggregate Level Variables (number of actions, total response time)

Item ID	Number of Actions					Response Time (Minutes)				
	Median	Mean	SD	Min	Max	Median	Mean	SD	Min	Max
U19a	15	15.85	11.76	0	97	1.80	2.08	1.40	0.09	20.58
U19b	11	17.80	24.28	0	260	2.83	3.24	2.49	0.08	26.37
U07x	13	14.24	12.00	0	90	1.66	1.88	1.29	0.05	9.45
U02x	24	33.93	33.82	0	194	2.54	3.59	3.48	0.09	45.07
U16x	14	20.07	21.25	0	191	1.85	2.26	1.83	0.06	15.93
U11b	15	24.15	27.54	0	271	1.21	1.59	1.49	0.06	19.43
U23x	12	15.88	16.02	0	183	1.36	1.66	1.72	0.07	42.25

Note: The items are presented in the order of their position in PS2.



- In each item, individual was assigned to the quadrant based on the number of actions and total response time compared with the median value of the whole sample in this item.
- For those showing in the same quadrant across more than half the assigned items (i.e., 4 out of 7 items), they were identified as consistent pattern and labeled as the corresponding quadrant (G1-G4), otherwise they were assigned in the inconsistent group (G5).

$$Q_1 = \{1, 2, 1, 3, 1, 1, 1\}$$

$$G = \{5, 1, 1, 0\}$$

$$Q_2 = \{1, 2, 1, 3, 4, 4, 3\}$$

$$G = \{2, 1, 2, 2\}$$

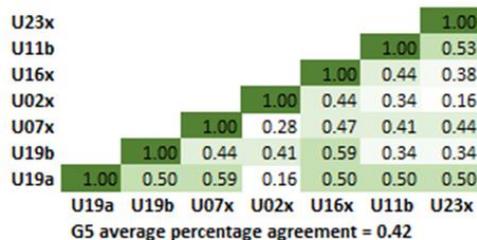
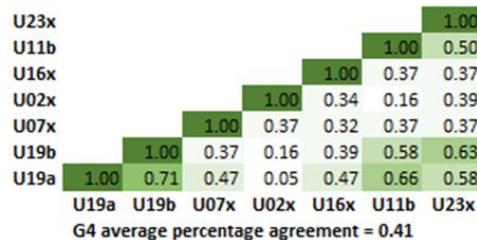
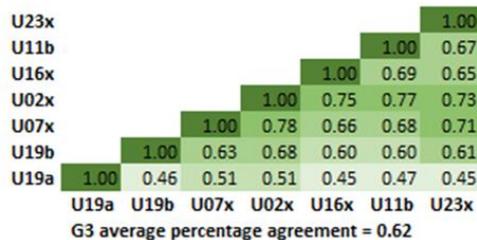
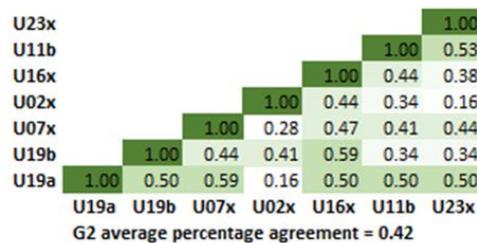
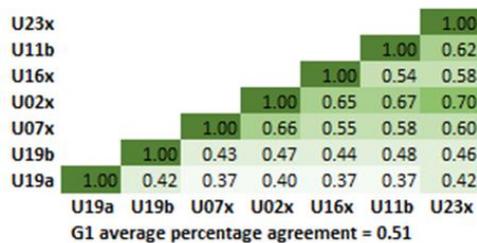
Study 1: Using Aggregate Level Variables (number of actions, total response time)

	G1	G2	G3	G4	G5
	A+T+	A-T+	A-T-	A+T-	
Number of respondents	488	32	477	38	302
Percentage	36.5%	2.4%	35.7%	2.8%	22.6%

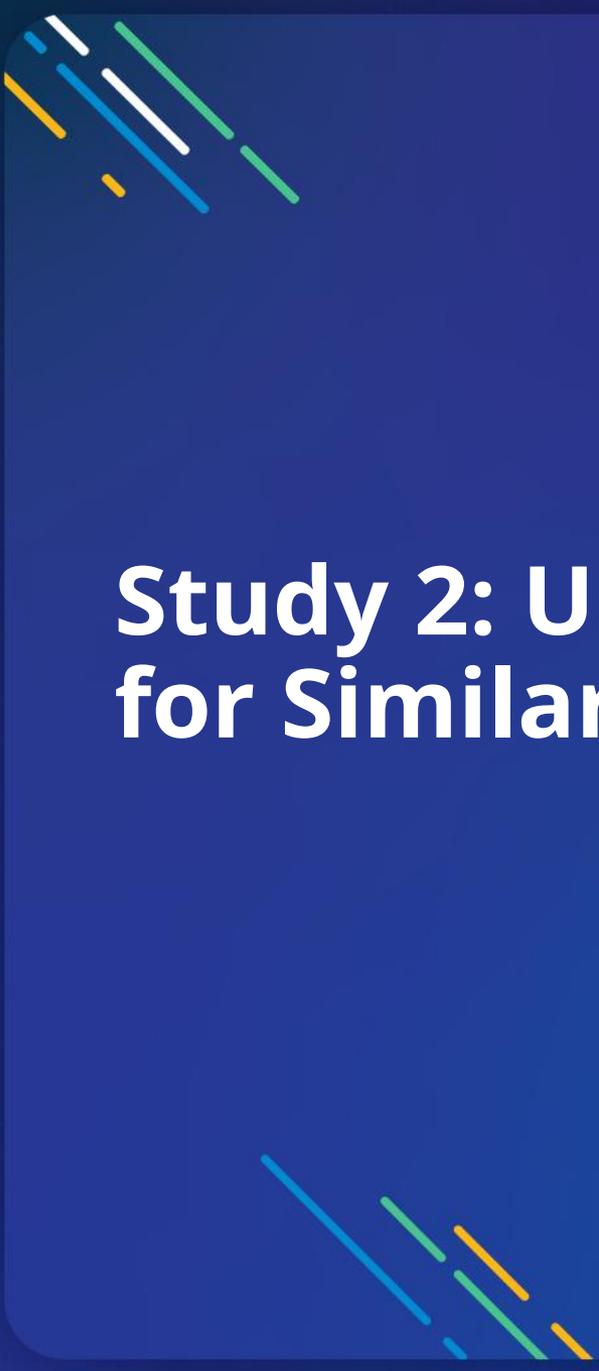
Note: G1 to G4 represent consistent behavioral groups, while G5 represent inconsistent behavioral group. G1 indicates the group with long action sequences and long time, G2 indicates the group with short action sequences and long time, G3 indicates the group with short action sequences and short time, and G4 indicates the group with long action sequences and short time.

Study 1: Using Aggregate Level Variables (number of actions, total response time)

Percentage agreement by five (in)consistency groups



- Respondents using short action sequence and short response time were the most consistent across multiple items.
- Respondents (A-T+ or A+T-) were less stable to remain in the same quadrant across items.



Study 2: Using Action Sequences for Similarity Computation



Study 2: Using Action Sequences for Similarity Computation

- Generating process sequence indicators across multiple tasks
- Sequence distance between individual observed sequence (OS) and predefined reference sequences (RS) with longest common subsequences (LCS; He et al., 2021)

Longest common subsequence

		j							
		0	1	2	3	4	5	6	
		y _j B D C A B A							
i	0	x _i	0	0	0	0	0	0	0
	1	A	0	↑	↑	↑	↖	←	↖
	2	B	0	↖	←	←	↑	↖	←
	3	C	0	↑	↑	↖	←	↑	↑
	4	B	0	↖	↑	↑	↑	↖	←
	5	D	0	↑	↖	↑	↑	↑	↑
	6	A	0	↑	↑	↑	↖	↑	↖
	7	B	0	↖	↑	↑	↑	↖	↑

Let $X = (x_1, x_2, \dots, x_i)$ and $Y = (y_1, y_2, \dots, y_j)$ be two sequences. x_i and y_j are actions within the sequence X and Y , respectively. The prefixes of X and Y are X_1, X_2, \dots, X_i and Y_1, Y_2, \dots, Y_j , respectively. Let $LCS(X_i, Y_j)$ represent the set of longest common subsequence of prefixes X_i and Y_j . The set of sequences is given as:

$$LCS(X_i, Y_j) = \begin{cases} \emptyset & \text{if } i = 0 \text{ or } j = 0 \\ LCS(X_{i-1}, Y_{j-1}), x_i & \text{if } x_i = y_i \\ \text{longest}(LCS(X_i, Y_{j-1}), LCS(X_{i-1}, Y_j)) & \text{if } x_i \neq y_i \end{cases}$$

$$\text{length}(LCS(X_i, Y_j)) = \begin{cases} 0 & \text{if } i = 0 \text{ or } j = 0 \\ \text{length}(i-1, j-1) + 1 & \text{if } x_i = y_i \\ \max(\text{length}(i, j-1), \text{length}(i-1, j)) & \text{if } x_i \neq y_i \end{cases}$$

$$LCS(X, Y) = \text{longest}(LCS(X_i, Y_{k_j}))$$

LCS Computation Example

RS_1: searching from toolbar (length=11)

Start, Toolbar_SS_Find, On_SearchBox, Off_SearchBox, Search_OK, SS_SEARCH, Email, On_Email_Message, Off_Email_Message, Next, Next_OK

RS_2: searching from menu item (length=11)

Start, MenuItem_Find, On_SearchBox, Off_SearchBox, Search_OK, SS_SEARCH, Email, On_Email_Message, Off_Email_Message, Next, Next_OK

RS_3: sorting from toolbar (length=9)

Start, Toolbar_SS_Sort, Sort_1_B, Sort_OK, Email, On_Email_Message, Off_Email_Message, Next, Next_OK

RS_4: sorting from menu item (length=9)

Start, MenuItem_Sort, Sort_1_B, Sort_OK, Email, On_Email_Message, Off_Email_Message, Next, Next_OK

OBSERVATION (length=25)

Start, Toolbar_SS_Help, Menu_SS_Edit, Menu_SS_Data, MenuItem_Sort, Sort_1_B, Sort_1A, Sort_OK, SS_Sort_1Ba, Email, On_Email_Message, Off_Email_Message, SS, On_Email_Message, Off_Email_Message, Email, On_Email_Message, Off_Email_Message, Off_Email_Message, Toolbar_E_Send, On_Email_Message, Off_Email_Message, Next, On_Email_Message, Off_Email_Message, Next_OK

LCS1 (length=6): Start, Email, On_Email_Message, Off_Email_Message, Next, Next_OK

LCS2 (length=6): Start, Email, On_Email_Message, Off_Email_Message, Next, Next_OK

LCS3 (length=8): Start, Sort_1_B, Sort_OK, Email, On_Email_Message, Off_Email_Message, Next, Next_OK

LCS4 (length=9): Start, MenuItem_Sort, Sort_1_B, Sort_OK, Email, On_Email_Message, Off_Email_Message, Next, Next_OK

LCS Indicators

- Similarity

- $Similarity = \text{len}(LCS) / \text{len}(RS)$
- $SM = \text{Mean}(Sim_1, Sim_2, \dots, Sim_n)$
- $SSD = \text{SD}(Sim_1, Sim_2, \dots, Sim_n)$

- Efficiency

- $Efficiency = \text{len}(LCS) / \text{len}(OS)$
- $EM = \text{Mean}(Eff_1, Eff_2, \dots, Eff_n)$
- $ESD = \text{SD}(Eff_1, Eff_2, \dots, Eff_n)$

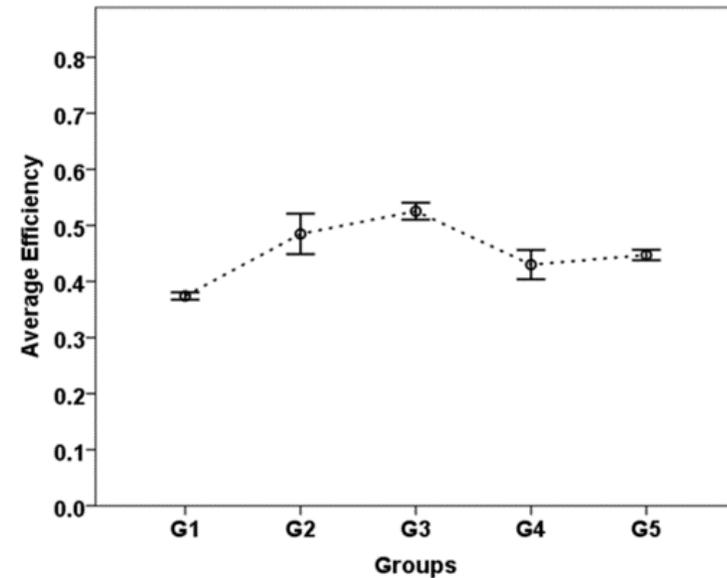
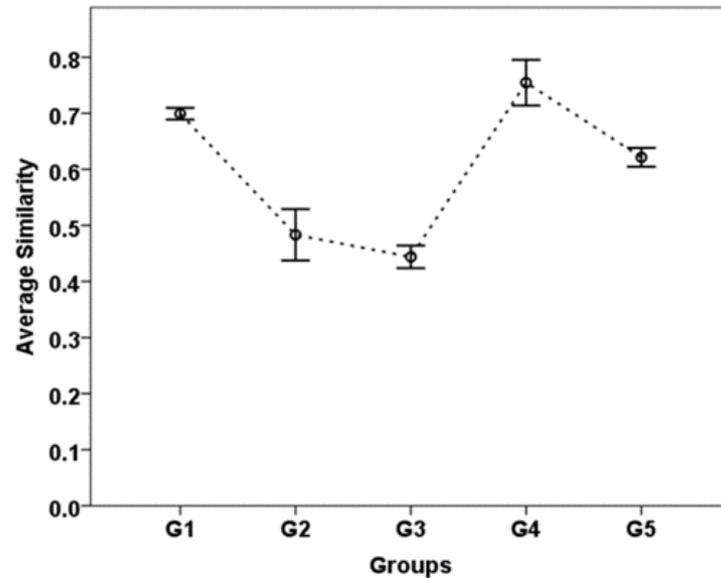
The mean of this distribution (SM) is defined as the average degree of similarity across items. A higher value of SM indicates that, on average, a respondent solved problems by following the reference sequences closely.

The standard deviation of this distribution (SSD) is used as an indicator of consistency of similarity to show how much the observed sequence is far away from the predefined ones.

The mean of this distribution (EM) is simply defined as the degree of efficiency across items. A higher value of EM indicates that a respondent on average solves problems in an efficient way (i.e., with few redundant actions).

The standard deviation of this distribution (ESD) is used as an indicator of consistency of efficiency that varies across items.

Study 2: Using Action Sequences for Similarity Computation



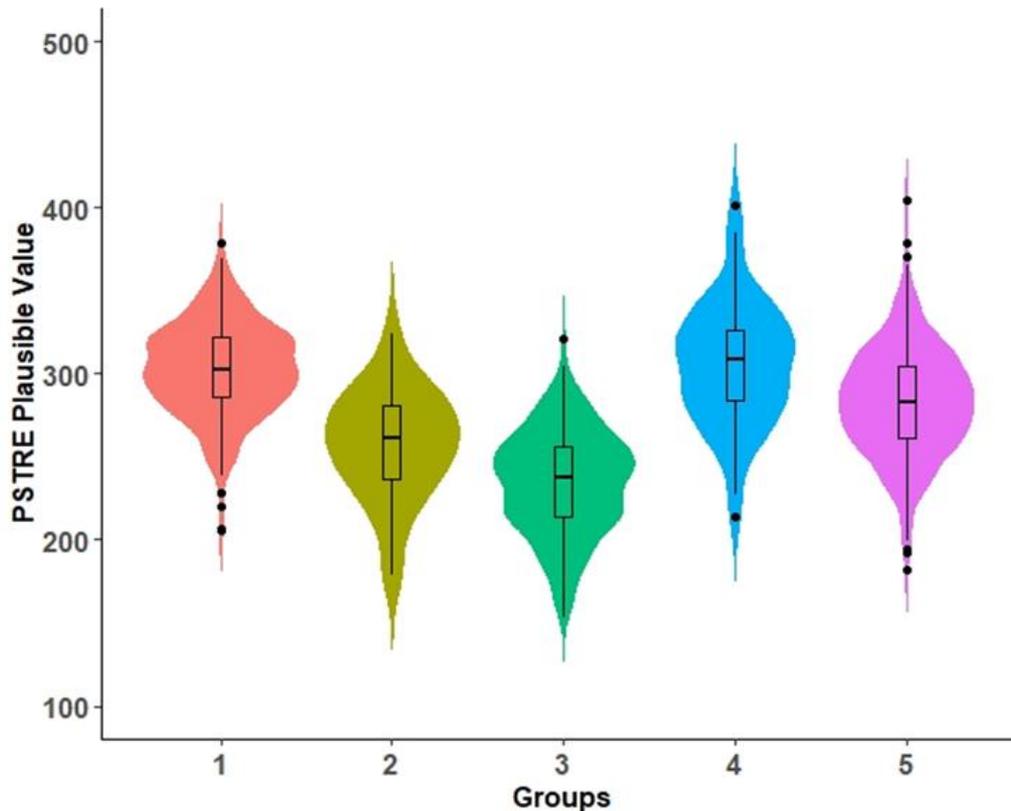
The association among two LCS indicators and (in)consistency groups derived from response time and number of actions



Study 3: Mapping Behavioral Patterns by Problem-Solving Competency and Background Variables



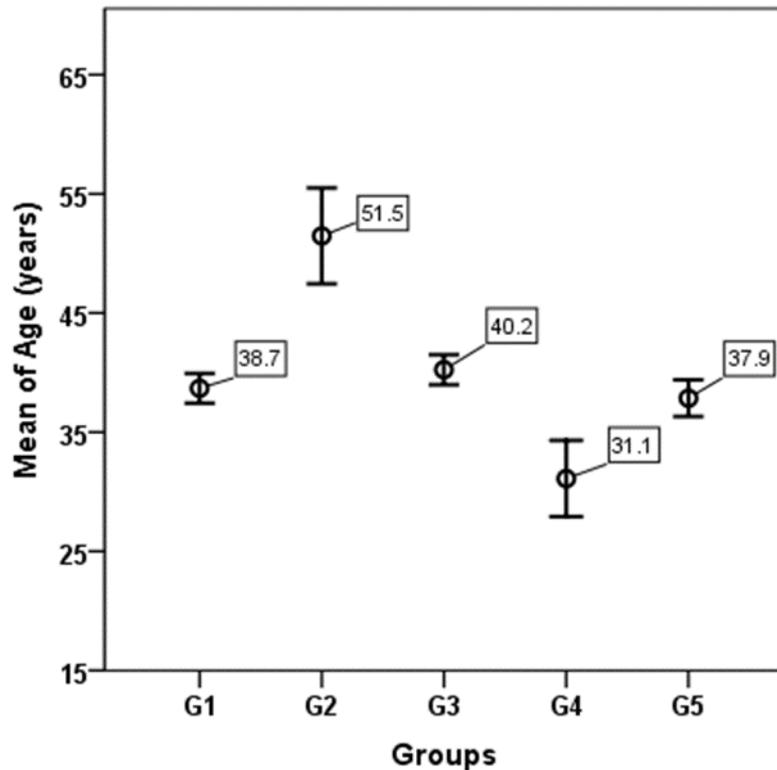
Study 3: Mapping Behavioral Patterns by Problem-Solving Competency and Background Variables



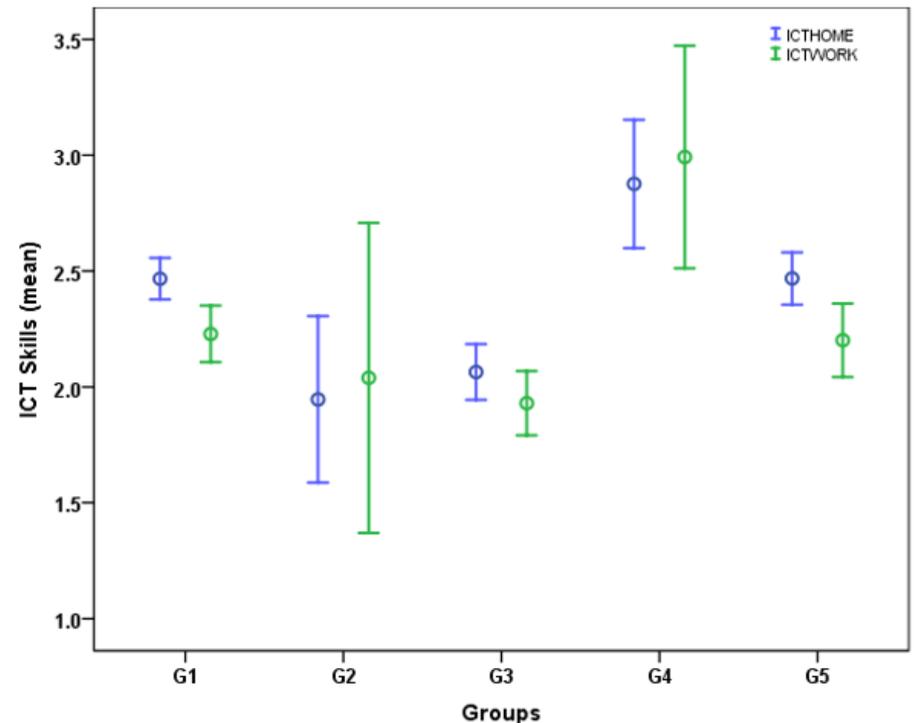
A bimodal distribution in G1 and G3, suggesting respondents in these groups possibly had mixed proficiency levels while having similar behaviors.

The distribution of problem-solving proficiency by five (in)consistency groups

Study 3: Mapping Behavioral Patterns by Problem-Solving Competency and Background Variables

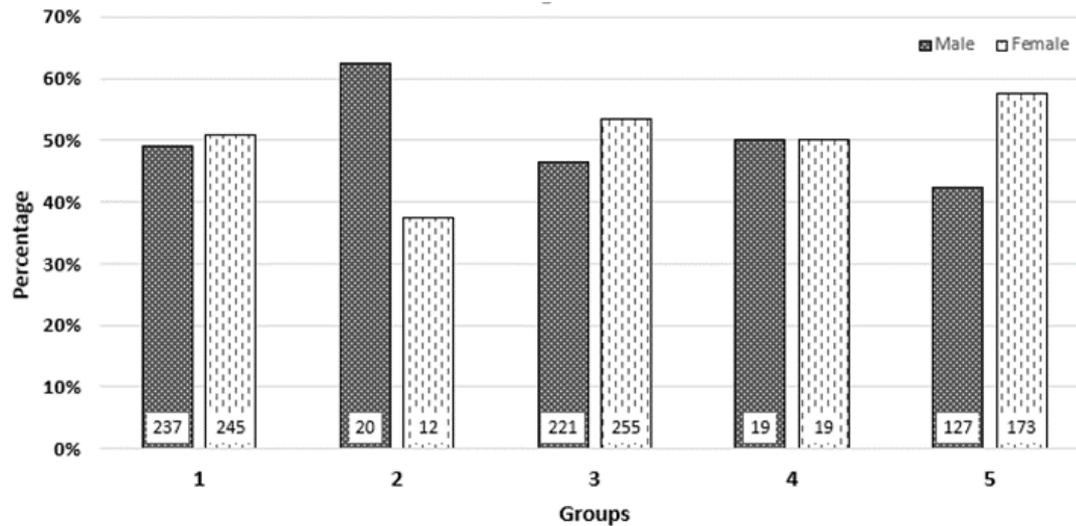


The distribution of age by behavioral patterns



The distribution of use of ICT at home and at work by behavioral patterns

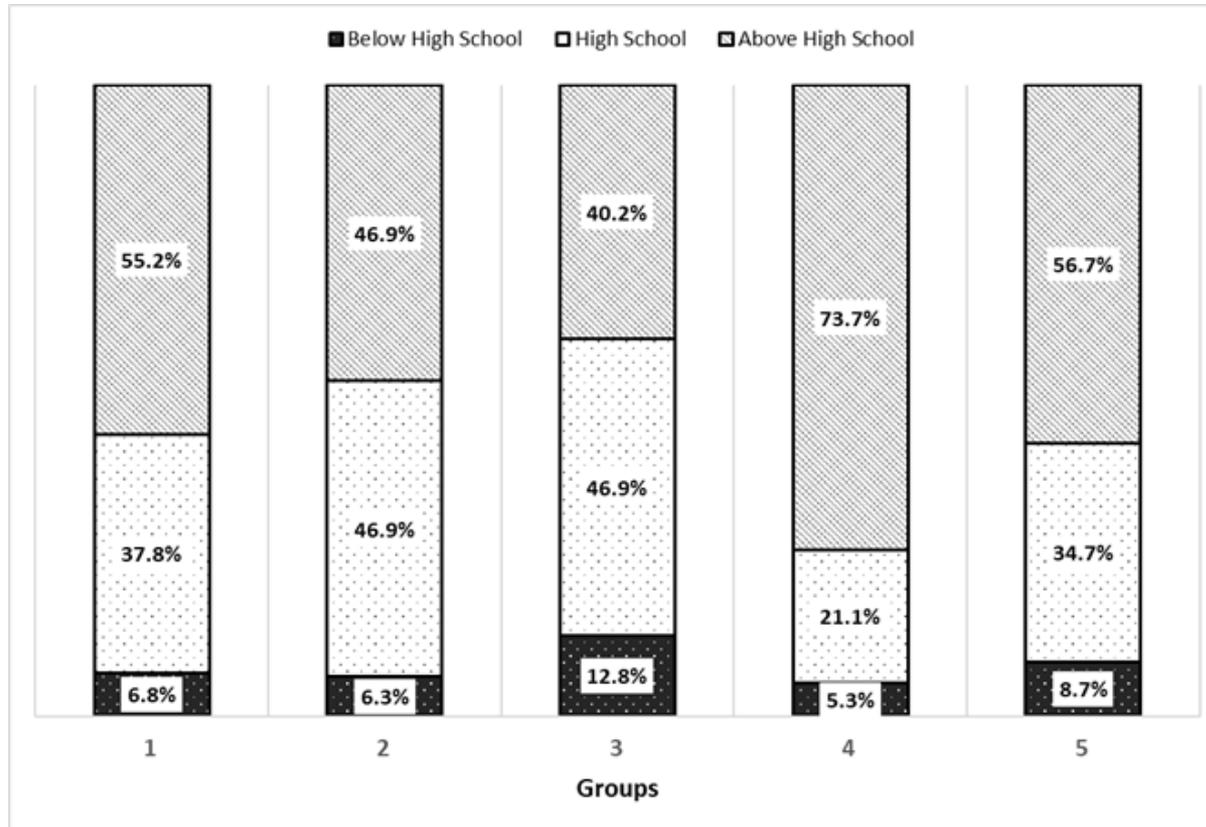
Study 3: Mapping Behavioral Patterns by Problem-Solving Competency and Background Variables



A higher proportion of males (over 60%) than females were found in the group consistently used short action sequences and long response times.

The distribution of gender by behavioral patterns

Study 3: Mapping Behavioral Patterns by Problem-Solving Competency and Background Variables



The distribution of respondents' educational level by behavioral patterns

Summary

- This study drew on the process aggregate-level variables and action sequences to assess the consistency of test-takers' behavior patterns across multiple interactive items, and also associated with competency level and background variables.
- Around 80% of respondents showed consistent patterns (in over half of the tasks) by the two dimensions, response time and the number of actions.
- Respondents who consistently followed A+T- pattern were found the highest problem-solving competency, the youngest, highest education level and adopted the most similar strategies with optimal sequences.
- From response processes, high-need groups could be identified for better attention for intervention (e.g., adults showing A-T+ may be highly motivated but need further support)

Discussion and Outlook



How Predictable the Process Variables in PUF?

- Dilemma:
 - How many variables and on which level of process data need to be released?
 - Research supports: the more the better?
 - Country: confidentiality, cost, operational work
 - Limited data could be released
- Three process variables in the public released file of PIAAC and PISA
 - Number of actions
 - Total time
 - Time for the first action

Machine Learning Binary Prediction

- Study 1: Use three process variables (number of actions, total time, time for the first action) in the PUF (n = 5,292, from 5 countries, focus on PS2)

	LR		RF		SVM	
	<i>Mean</i>	<i>SD</i>	<i>Mean</i>	<i>SD</i>	<i>Mean</i>	<i>SD</i>
Accuracy	0.81	0.02	0.84	0.01	0.83	0.00
Sensitivity	0.84	0.02	0.85	0.01	0.85	0.01
Specificity	0.77	0.02	0.82	0.02	0.79	0.02
PPV	0.83	0.01	0.86	0.01	0.85	0.01
NPV	0.78	0.02	0.81	0.01	0.80	0.01
F1	0.84	0.02	0.86	0.01	0.85	0.00
AUROC	0.88	0.02	0.92	0.00	0.90	0.00

Note. LR = logistic regression; RF = random forest; SVM = support vector machine; PPV = positive predictive value; NPV = negative predictive value; AUC = area under the ROC curve; BLv1 = below level 1; Lv1 = level 1; Lv2 = Level 2; Lv3 = Level 3.

Machine Learning Binary Prediction

- Study 2: Use two generated variables similarity and efficiency (n = 5,292, from 5 countries, focus on PS2)

	LR		RF		SVM	
	<i>Mean</i>	<i>SD</i>	<i>Mean</i>	<i>SD</i>	<i>Mean</i>	<i>SD</i>
Accuracy	0.83	0.01	0.83	0.01	0.83	0.01
Sensitivity	0.77	0.02	0.78	0.02	0.78	0.02
Specificity	0.87	0.01	0.86	0.02	0.87	0.01
PPV	0.81	0.01	0.81	0.02	0.82	0.02
NPV	0.84	0.01	0.84	0.01	0.84	0.01
F1	0.79	0.01	0.79	0.00	0.80	0.01
AUROC	0.91	0.01	0.91	0.01	0.91	0.01

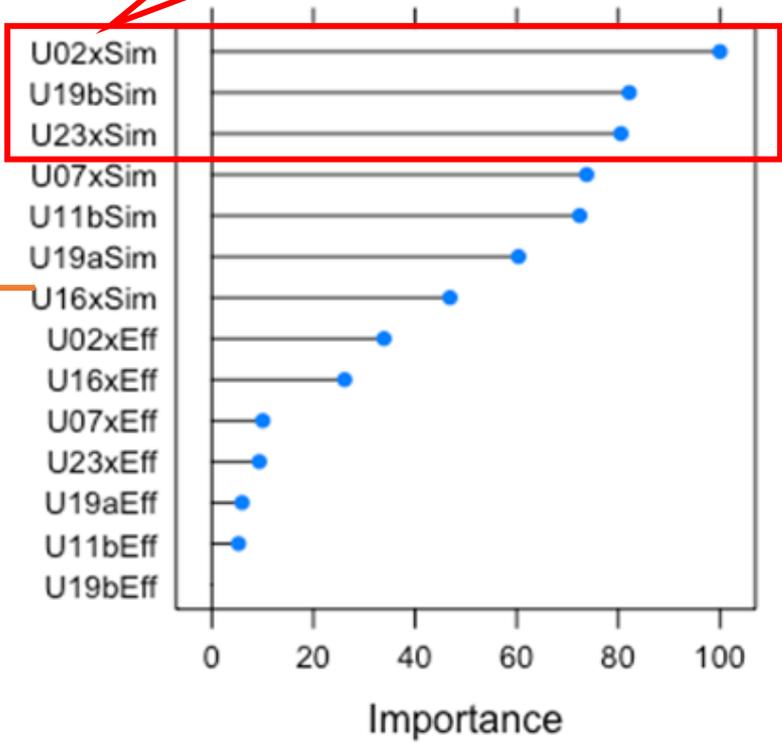
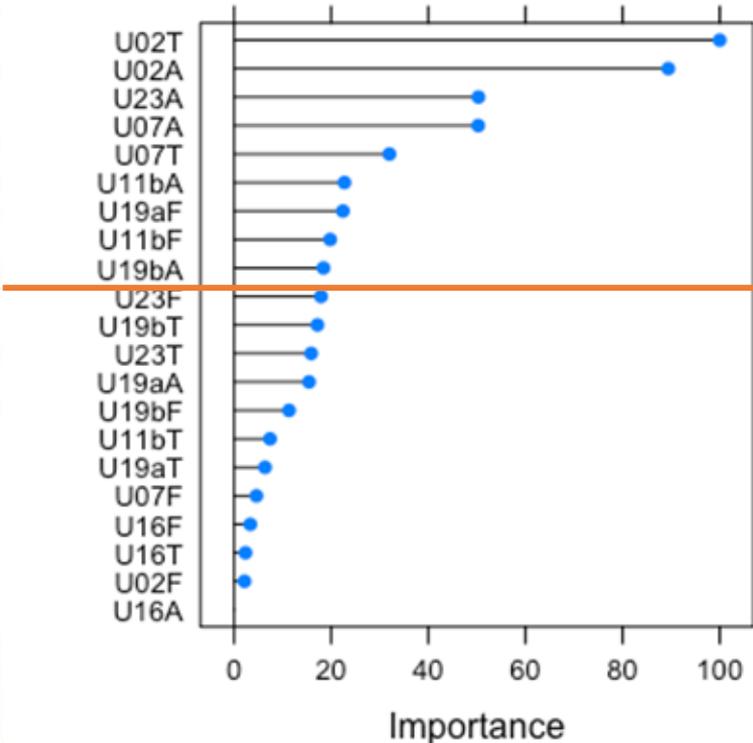
Note. LR = logistic regression; RF = random forest; SVM = support vector machine; PPV = positive predictive value; NPV = negative predictive value; AUC = area under the ROC curve; BLv1 = below level 1; Lv1 = level 1; Lv2 = Level 2; Lv3 = Level 3.

Machine Learning Binary Prediction

- Importance of variables

	<i>a</i>	<i>b</i>
Unit 19a	1.414	-1.367
Unit 19b	1.072	-0.677
Unit 07	1.104	-0.237
Unit 02	1.184	0.784
Unit 16	1.377	-0.773
Unit 11b	0.471	0.774
Unit 23	0.533	-0.052

The items with high discrimination in behaviors (not necessary to be highly discriminative ones in IRT model).



Implications

- The three process variables (number of actions, total time, time for the first action) are very predictive (over 80% accuracy) to distinguish low and high adults with problem-solving skill. These three variables need to continue included in the PUF.
- The generated variable similarity (distance measure between observed sequence and predefined sequence) is a very predictive variable and also could be considered to use in further operational work and recommended to be included in the PUF. (would need content experts' help).
- The importance of variables in prediction could be used as an efficient way to identify the high-discriminative items from process data perspective, (not necessary to be consistent as item discrimination parameters estimated in IRT), which could be helpful in interactive problem-solving items design.

Final Words

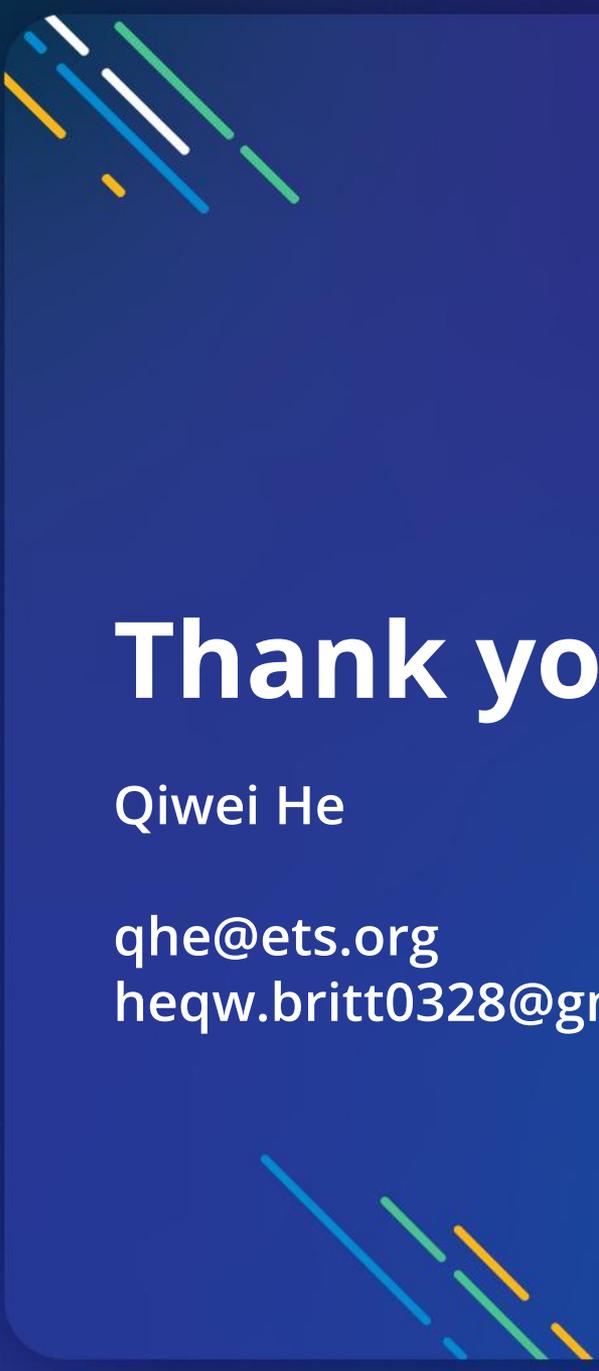
- Process data has been arousing increasing interests and attention in educational assessment and learning analytics.
- One-time assessment is not the target of education but tracking the students' progress and providing helpful supports. Process data could be given a broader scope for dynamic and longitudinal study.
- Post-assessment process data analysis could be progressed to dynamic process data analysis throughout the assessment. It could be a new trend in the future studies to bring new meaning for adaptive testing, not only from responses but also from interactions.

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